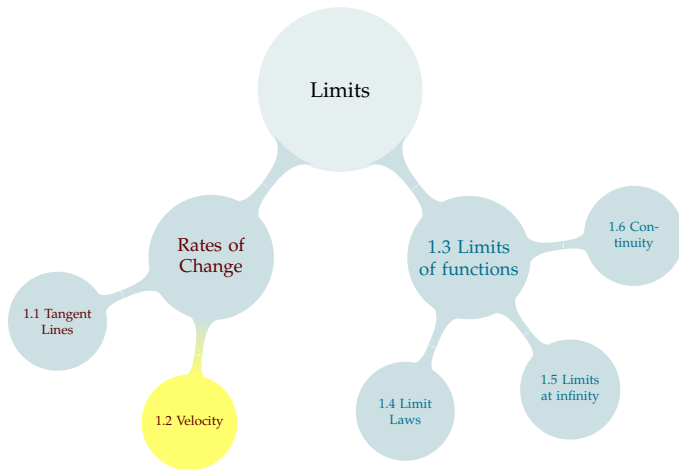
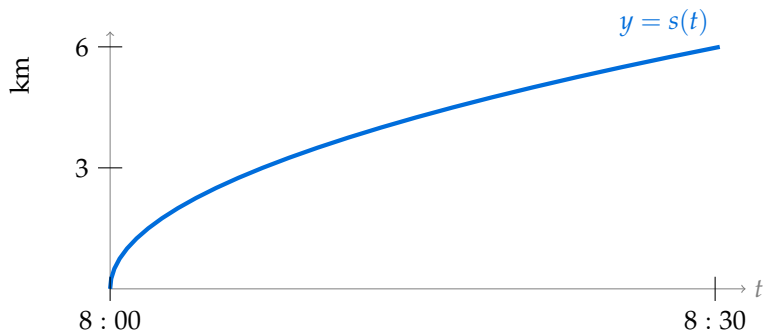
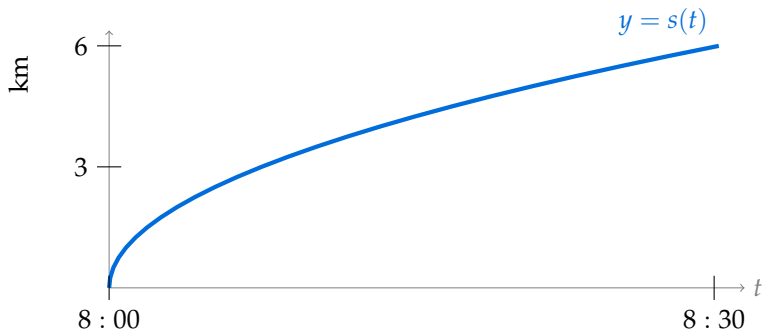


TABLE OF CONTENTS

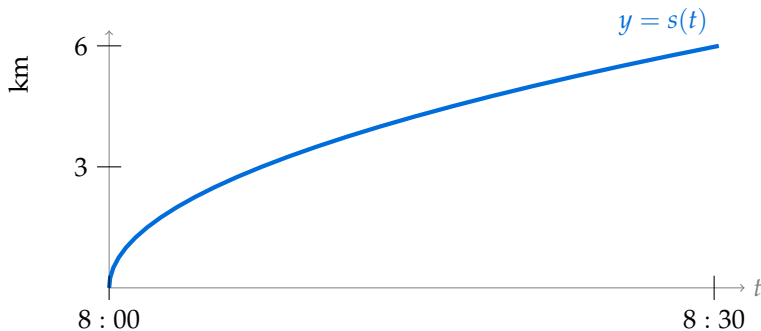






It took $\frac{1}{2}$ hour to bike 6 km. 12 kph represents the:

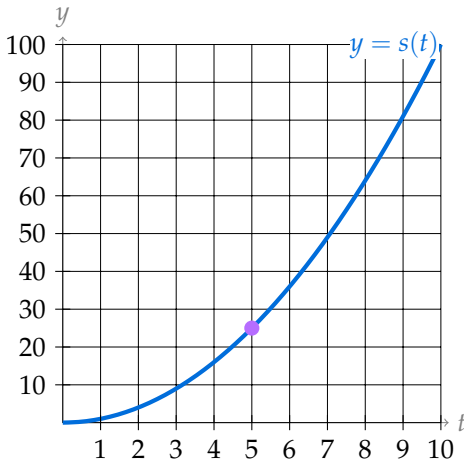
- A. secant line to $y = s(t)$ from $t = 8:00$ to $t = 8:30$
- B. slope of the secant line to $y = s(t)$ from $t = 8:00$ to $t = 8:30$
- C. tangent line to $y = s(t)$ at $t = 8:30$
- D. slope of the tangent line to $y = s(t)$ at $t = 8:30$



At 8:25, the speedometer on my bike reads 5 kph. 5 kph represents the:

- A. secant line to $y = s(t)$ from $t = 8 : 00$ to $t = 8 : 25$
- B. slope of the secant line to $y = s(t)$ from $t = 8 : 00$ to $t = 8 : 25$
- C. tangent line to $y = s(t)$ at $t = 8 : 25$
- D. slope of the tangent line to $y = s(t)$ at $t = 8 : 25$

Suppose the distance from the ground s (in meters) of a helium-filled balloon at time t over a 10-second interval is given by $s(t) = t^2$. Try to estimate how fast the balloon is rising when $t = 5$.



Let's look for an algebraic way of determining the velocity of the balloon when $t = 5$.

OUR FIRST LIMIT

Average Velocity, $t = 5$ to $t = 5 + h$:

$$\begin{aligned}\frac{\Delta s}{\Delta t} &= \frac{s(5+h) - s(5)}{h} \\ &= \frac{(5+h)^2 - 5^2}{h} \\ &= 10 + h \quad \text{when } h \neq 0\end{aligned}$$

When h is very small,

$$\text{Vel} \approx 10$$

LIMIT NOTATION

We write:

$$\lim_{h \rightarrow 0} (10 + h) = 10$$

We say: “The limit as h goes to 0 of $(10 + h)$ is 10.”

It means: As h gets extremely close to 0, $(10 + h)$ gets extremely close to 10.