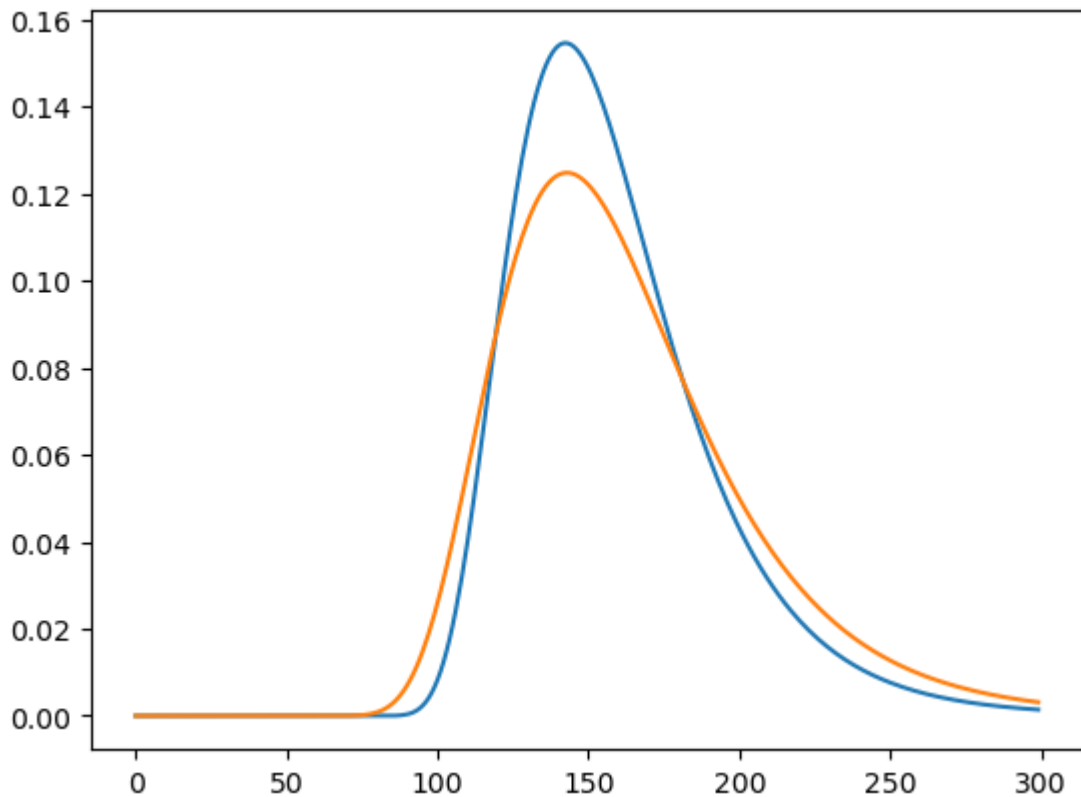


## Likelihood calculations and plots for question 3

```
In [ ]: def L(n):  
        if n<76: return 0  
        return binomial(40,14)*binomial(n-40,36)/binomial(n,50)  
  
        def L_rep(n):  
            if n<40: return 0  
            return binomial(50,14)* (40/n)**14 * (1-40/n)**36
```

```
In [2]: plot([L(n) for n in range(300)], [L_rep(n) for n in range(300)])
```



Blue: Likelihood; Orange: Likelihood with repetition. Note that (unlike probabilities), the likelihoods do not add up to 1.

## Problem 6

```
In [ ]: def birthday_repeat(n,days_in_year=365):
        A = [randrange(days_in_year) for i in range(n)]
        #sets contain each element only once.
        return len(set(A)) < len(A)

def birthday_sample(n_people,n_tests,days_in_year=365):
    return sum(birthday_repeat(n_people,days_in_year) for i in range(n_tests))

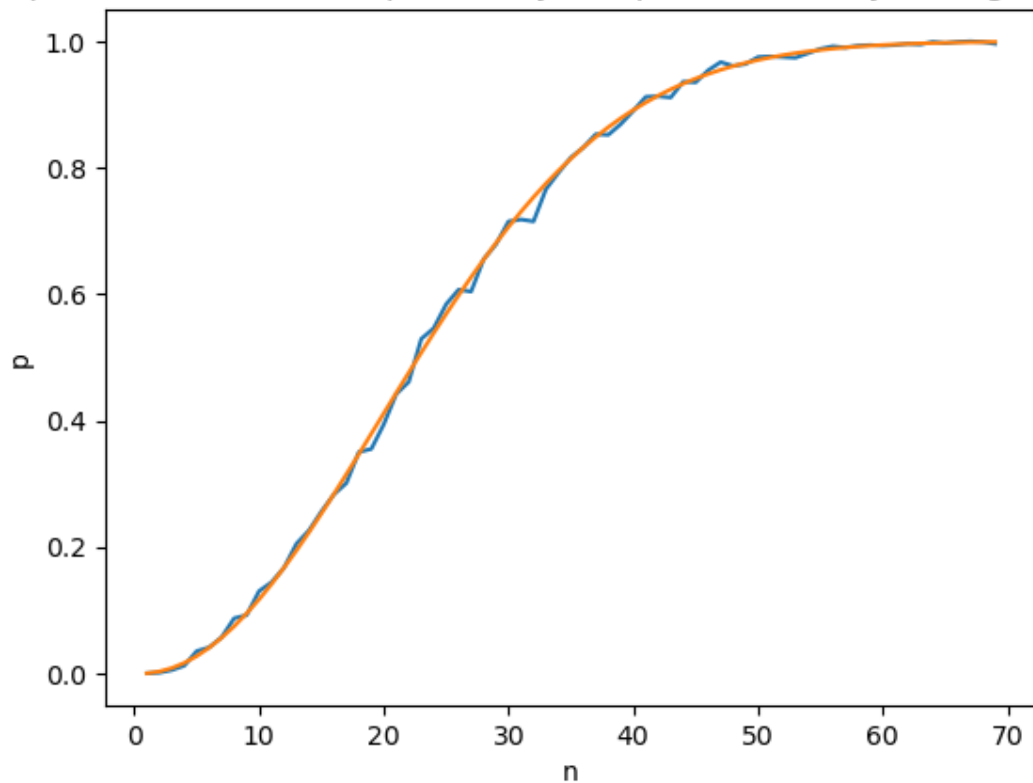
def repeat_prob(n,days_in_year=365):
    return 1 - factorial(days_in_year) / factorial(days_in_year-n) / days_in
```

```
In [ ]: X = range(1,70)
        Y = [birthday_sample(n,1000) for n in X]
        Z = [repeat_prob(n) for n in X]
```

```
In [10]: plt.figure()
         plt.plot(X,Y)
         plt.plot(X,Z)
         plt.xlabel('n')
         plt.ylabel('p')
         plt.title('Experimental and actual probability of repeated birthday among n
```

```
Out[10]: Text(0.5, 1.0, 'Experimental and actual probability of repeated birthday among n people')
```

Experimental and actual probability of repeated birthday among n people



```
In [11]: X = range(1,70)
         Y_mars = [birthday_sample(n,1000,669) for n in X]
         Z_mars = [repeat_prob(n,669) for n in X]
```

```
In [12]: plt.figure()  
plt.plot(X,Y_mars)  
plt.plot(X,Z_mars)  
plt.xlabel('n')  
plt.ylabel('p')  
plt.title('Experimental and actual probability of repeated birthday among n
```

```
Out[12]: Text(0.5, 1.0, 'Experimental and actual probability of repeated birthday among n Martians')
```

Experimental and actual probability of repeated birthday among n Martians

