Midterm 2 November 18, 2015 Duration: 50 minutes This test has 5 questions on 8 pages, each worth 8 points, for a total of 40 points.

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- Read all the questions carefully before starting to work.
- Give complete arguments and explanations for all your calculations. Answers without justifications will not be marked.
- Attempt to answer all questions for partial credit.
- This is a closed-book examination. No aids of any kind are allowed, including: documents, cheat sheets, electronic devices (including calculators, phones, etc.)

Student No.:

_ Section: _____

Signature: ___

Question:	1	2	3	4	5	Total
Points:	8	8	8	8	8	40
Score:						

Student Conduct during Examinations					
 Each examination candidate must be prepared to produce, upon the request of the invigilator or examiner, his or her UBCcard for identification. 	 (ii) purposely exposing written papers to the view of other ex amination candidates or imaging devices; 				
2. Examination candidates are not permitted to ask questions of the	(iii) purposely viewing the written papers of other examinatio candidates;				
examiners or invigilators, except in cases of supposed errors or am- biguities in examination questions, illegible or missing material, or the like.	 (iv) using or having visible at the place of writing any books, pa pers or other memory aid devices other than those authorized by the examiner(s); and, 				
3. No examination candidate shall be permitted to enter the examina- tion room after the expiration of one-half hour from the scheduled starting time, or to leave during the first half hour of the examina- tion. Should the examination run forty-five (45) minutes or less, no examination candidate shall be permitted to enter the examination room once the examination has begun.	(v) using or operating electronic devices including but not lim ited to telephones, calculators, computers, or similar device other than those authorized by the examiner(s)(electronic de vices other than those authorized by the examiner(s) must b completely powered down if present at the place of writing)				
4. Examination candidates must conduct themselves honestly and in accordance with established rules for a given examination, which will be articulated by the examiner or invigilator prior to the exam- ination commencing. Should dishonest behaviour be observed by the examiner(s) or invigilator(s), pleas of accident or forgetfulness	 Examination candidates must not destroy or damage any examin tion material, must hand in all examination papers, and must n take any examination material from the examination room witho permission of the examiner or invigilator. Notwithstanding the above, for any mode of examination that do not fall into the traditional, paper-based method, examination ca didates shall adhere to any special rules for conduct as establishe and articulated by the examiner. 				
shall not be received.5. Examination candidates suspected of any of the following, or any other similar practices, may be immediately dismissed from the examination by the examiner/invigilator, and may be subject to disciplinary action:					
 speaking or communicating with other examination candi- dates, unless otherwise authorized; 	 Examination candidates must follow any additional examination rules or directions communicated by the examiner(s) or invigilator(s). 				

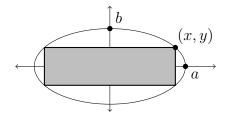
8 marks 1. Find all critical points of

$$f(x,y) = x^3 + y^3 - 12xy,$$

and classify each critical point as a local maximum, a local minimum, or a saddle point.

8 marks2. Using Lagrange multipliers, determine the area of the largest rectangle (with sides parallel
to the x and y axes) that can be inscribed in the ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1.$$



2 marks 3. (a) Let $f(x, y) = y^4 \sin x$. Find the gradient $\vec{\nabla} f$.

Answer:

2 marks

(b) Calculate the directional derivative for f at the point $(\frac{\pi}{2}, 1)$ in the direction given by $\vec{u} = \langle 2, 1 \rangle$.

Answer:

2 marks

(c) Still considering the point $(\frac{\pi}{2}, 1)$, determine the (normalized) direction or directions in which f is changing at rate 2.

Answer:

2 marks

(d) What is the maximal rate of change of f at the point $(\frac{\pi}{2}, 1)$, and in what (normalized) direction is this maximal rate of change achieved?

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Work on this page will *not* be marked unless you make clear indication on the original question page.

4. Consider the integral

 $\int_0^1 \int_y^1 e^{x^2} \, dx \, dy.$

4 marks

(a) Sketch the integration region and write the integral in reversed order.

Answer:

4 marks

(b) Using the result of part (a), evaluate the integral.

5. Consider the solid which lies under the surface $z = 1 + x^2y^2$ and above the region in the x-y plane bounded by $x = y^2$ and x = 4.

4 marks

(a) Write down (but don't evaluate) a double integral whose value gives the volume of the solid.

Answer:

4 marks (b) Ev

(b) Evaluate the integral to determine the volume of the solid.

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Work on this page will *not* be marked unless you make clear indication on the original question page.