ACKNOWLEDGMENT

UBC's Point Grey Campus is located on the traditional, ancestral, and unceded territory of the $x^w m \theta \theta k^w \theta \psi \theta m$ (Musqueam) people. The land it is situated on has always been a place of learning for the Musqueam people, who for millennia have passed on in their culture, history, and traditions from one generation to the next on this site.

Course Information

| Course Title | Course Code Number | Credit Value |
|------------------------|--------------------|--------------|
| Multivariable Calculus | Math 253 | 3 |

Prerequisites

Pre-reqs: Whatever the official regulations and calendar say.

CONTACTS

| Section | Course Instructor(s) | Contact Details | Office Hours |
|---------|----------------------|-------------------------------|--------------|
| | Colin Macdonald | <pre>cbm[at]math.ubc.ca</pre> | TBA |

See Canvas for alternative ways to contact us including discussion forums if your question is of general interest.

OTHER INSTRUCTIONAL STAFF

Other people (such as teaching assistants) are also involved in the teaching of this course. You may meet some of them over the course of the term and/or interact with them online. However, any concerns about grading should come to your instructors via mechanisms outlined on Canvas (namely, the grade change request form).

Course Structure

The instructional format for the course will consist mainly of lectures at the scheduled times. Most lectures will be delivered in-person, although its possible that a lecture might be delivered online (in this case, as much advanced warning as possible will be given). Students are expected to participate in the regularly-scheduled lectures for their section.

There will be WeBWorK and PrairieLearn homework to help you practice technical skills and also develop understanding of the main concepts. You are encouraged to be active on our forums (such as Piazza or other technologies)—asking questions and providing answers (and generally discussing mathematics with your colleagues) is an excellent way to learn!

SCHEDULE OF TOPICS

This is an approximate week-by-week outline of topics for the course. An online version on Canvas will be updated as the course progresses.

| Order | Topics | CLP-3 Sections |
|-------|--|-----------------------|
| 1 | Three-dimensional coordinate systems, vectors, dot product | 1.1, 1.2.1, 1.2.2 |
| 2 | cross product, equations of lines and planes | 1.2.5, 1.4, 1.5 |
| 3 | Curves and their tangent vector, cylinders and quadric | 1.6, 1.7, 1.8, 1.9 |
| | surfaces, functions of several variables: domain, range, | |
| | graphs, level curves/surfaces | |
| 4 | Limits and continuity, partial derivatives | 2.1, 2.2, 2.3 |
| 5 | Chain rule, tangent planes and linear approximations | 2.4, 2.5, 2.6 |
| 6 | Directional derivatives and the gradient vector | 2.7 |
| 7 | Maximum and minimum values, Lagrange multipliers | 2.9, 2.10 |
| 8 | Double integrals over rectangles | 3.1 |
| 9 | Double integrals over general regions, double integrals in | 3.1, 3.2 |
| | polar coordinates | |
| 10 | Applications of double integrals | 3.3 |
| 11 | Surface area, triple integrals | 3.4, 3.5 |
| 12 | Triple integrals in cylindrical coordinates | 3.6 |
| 13 | Triple integrals in spherical coordinates | 3.7 |

LEARNING OUTCOMES

Multivariable calculus provides the language and tools to analyze outcomes that depend on more than one parameter (i.e., most situations in our world). Multivariable calculus is used in many fields of natural science, social science, computer science, and (obviously most importantly) engineering.

The main goal of the course is to develop an understanding of the fundamental concepts of multivariable calculus and the skills necessary for its applications. Upon completion of this course, students should be able to:

- 1. Manipulate vectors to perform geometric calculations in three dimensions.
- 2. Calculate, interpret, and apply derivatives of functions of several variables.
- 3. Integrate functions of several variables.

Learning Activities and Assessments of Learning

The course mark will be based on WeBWorK homework assignments (5%), PrairieLearn homework assignments (5%), quizzes (30%), and the final exam (60%). The final exam covers material from the entire course.

Homework and Forums There will be online homework which must be accessed from the common Canvas page. The main goal of the homework is to help you learn the material. You are encouraged to work in groups on the more difficult problems, but then complete your individualized problems yourself. Please do post questions and answers about homework (and other parts of the course) on our forums, but when posting the answers, refrain from solving the problem completely, instead, point out relevant ideas from the course or suggest the next step, etc.

We will drop the *lowest* WeBWorK score. We will drop the *lowest* PrairieLearn score. These cover incidents involving time-zone miscalculations, flaky internet, very-busy-this-week, etc. No further concessions are generally possible.

Quizzes There will some number of quizzes, the dates of which are subject to change but will be announced near the start of the term and posted on Canvas. Generally, you will write these quizzes either in scheduled class time or at self-scheduled times via UBC's Computer-Based Testing Facility. Please be aware of Student Conduct during Examinations.

Concessions There will be no make-up quizzes, and no late homework will be accepted. Students with concessions will have the weight of a test transferred to other aspects of the course, usually the final exam. You can receive **one** concession during the term by submitting the concession request form (it can be downloaded at: https://www.math.ubc.ca/undergraduate/advising-and-resources/exams) to your instructor. Further concessions or missed final exams need to be discussed with the Academic Advisors of your Faculty. There cannot be exceptions to these university-wide policies. Please note there are *already* mechanisms mentioned earlier and it is anticipated that these should cover all but the very rarest concession circumstances.

Final Exam The final exam will be scheduled during the standard examination period. Please be aware of Student Conduct during Examinations.

Scaling Grades may be scaled to be in line with historical standards and to ensure fairness across the sections. No scaling will be decided upon until all assessments are completed.

LEARNING MATERIALS

All course materials are available online at no cost and some are under free licenses that explicitly allow reuse or encourage community development.

- Lectures will happen during scheduled class time. Course information, materials and resources for all sections can be found on the common Canvas page.
- Our main discussion forum is Piazza.

ACADEMIC INTEGRITY

The academic enterprise is founded on honesty, civility, and integrity. As members of this enterprise, all students are expected to know, understand, and follow the codes of conduct regarding academic integrity. At the most basic level, this means submitting only original work done by you and acknowledging all sources of information or ideas and attributing them to others as required. This also means you should not cheat, copy, or mislead others about what is your work. Violations of academic integrity (i.e., misconduct) lead to the breakdown of the academic enterprise, and therefore serious consequences arise and harsh sanctions are imposed. Be sure you understand UBC's expectations: see the UBC Calendar entries on "Academic Honesty", "Academic Misconduct", and "Disciplinary Measures".

General policies of the mathematics department at listed at https://www.math.ubc.ca/general-syllabus-information

University Policies

UBC provides resources to support student learning and to maintain healthy lifestyles but recognizes that sometimes crises arise and so there are additional resources to access including those for survivors of sexual violence. UBC values respect for the person and ideas of all members of the academic community. Harassment and discrimination are not tolerated nor is suppression of academic freedom. UBC provides appropriate accommodation for students with disabilities and for religious observances. UBC values academic honesty and students are expected to acknowledge the ideas generated by others and to uphold the highest academic standards in all of their actions. Details of the policies and how to access support are available on the UBC Senate website.

LEARNING ANALYTICS

This course will be using the following learning technologies: Canvas, Piazza, WeBWorK, PrairieLearn, and perhaps others as needed. Many of these tools capture data about your activity and provide information that can be used to improve the quality of teaching and learning. In this course, we may use analytics data to:

- View overall class progress
- Track your progress in order, e.g., to provide you with feedback or advice
- Review statistics on course content being accessed to support improvements in the course
- Track participation in discussion forums
- Assess your participation in the course

This course generally avoids technologies that collect data primarily or secondarily for the profit of third-party entities. This should be considered an aspirational goal rather than a promise.

Copyright

All materials of this course (course handouts, notes, slides, assessments, readings, recordings, etc.) are either copyright of the Course Instructor or licensed to be used in this course by the copyright holder. Redistribution of these materials by any means without permission of the copyright holder(s) constitutes a breach of copyright and may lead to academic discipline. This sounds more draconian than the reality: many materials explicitly allow or encourage redistribution.

Lecture recordings, if provided, are for use by registered students only.

It would be at the very least *impolite* to record your colleagues without their permission. Your instructors' recordings—if provided—will strive to be respectful in this manner and we ask that you do the same.

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