

1. Find the third degree Maclaurin polynomial for  $f(x) = \sqrt{1+x}$ .

*Solution:* Since  $f(x) = (1+x)^{1/2}$ , we have  $f'(x) = (1/2)(1+x)^{-1/2}$ ,  $f''(x) = (-1/4)(1+x)^{-3/2}$ , and  $f'''(x) = (3/8)(1+x)^{-5/2}$ . So,  $f(0) = 1$ ,  $f'(0) = 1/2$ ,  $f''(0) = -1/4$ , and  $f'''(0) = 3/8$ , and the third-degree Maclaurin polynomial is

$$T_3(x) = 1 + (1/2)x - (1/4)x^2/2! + (3/8)x^3/3! = 1 + x/2 - x^2/8 + x^3/16$$