

Midterm Exam Duration: 50 minutes*This test has 5 questions on 7 pages, for a total of 35 points.*

- Read all the questions carefully before starting to work.
- All questions are long-answer; you should give complete arguments and explanations for all your calculations; answers without justifications will not be marked.
- Continue on the back of the previous page if you run out of space.
- Attempt to answer all questions for partial credit.
- This is a closed-book examination. **None of the following are allowed:** documents, cheat sheets or electronic devices of any kind (including calculators, cell phones, etc.)

First Name: _____ Last Name: _____

Student-No: _____

Signature: _____

Question:	1	2	3	4	5	Total
Points:	9	7	8	5	6	35
Score:						

Student Conduct during Examinations

1. Each examination candidate must be prepared to produce, upon the request of the invigilator or examiner, his or her UBCcard for identification.
2. Examination candidates are not permitted to ask questions of the examiners or invigilators, except in cases of supposed errors or ambiguities in examination questions, illegible or missing material, or the like.
3. No examination candidate shall be permitted to enter the examination room after the expiration of one-half hour from the scheduled starting time, or to leave during the first half hour of the examination. Should the examination run forty-five (45) minutes or less, no examination candidate shall be permitted to enter the examination room once the examination has begun.
4. Examination candidates must conduct themselves honestly and in accordance with established rules for a given examination, which will be articulated by the examiner or invigilator prior to the examination commencing. Should dishonest behaviour be observed by the examiner(s) or invigilator(s), pleas of accident or forgetfulness shall not be received.
5. Examination candidates suspected of any of the following, or any other similar practices, may be immediately dismissed from the examination by the examiner/invigilator, and may be subject to disciplinary action:
 - (i) speaking or communicating with other examination candidates, unless otherwise authorized;
 - (ii) purposely exposing written papers to the view of other examination candidates or imaging devices;
 - (iii) purposely viewing the written papers of other examination candidates;
 - (iv) using or having visible at the place of writing any books, papers or other memory aid devices other than those authorized by the examiner(s); and,
 - (v) using or operating electronic devices including but not limited to telephones, calculators, computers, or similar devices other than those authorized by the examiner(s)(electronic devices other than those authorized by the examiner(s) must be completely powered down if present at the place of writing).
6. Examination candidates must not destroy or damage any examination material, must hand in all examination papers, and must not take any examination material from the examination room without permission of the examiner or invigilator.
7. Notwithstanding the above, for any mode of examination that does not fall into the traditional, paper-based method, examination candidates shall adhere to any special rules for conduct as established and articulated by the examiner.
8. Examination candidates must follow any additional examination rules or directions communicated by the examiner(s) or invigilator(s).

Justify your answers and show all your work. Unless otherwise indicated simplification of answers is not required.

1. Compute the derivatives of the following functions

4 marks

(a)

$$f(x) = \frac{4}{\sqrt{x}} + 2e^x + 7e^\pi + \frac{x^3x^2}{x^4}$$

5 marks

(b)

$$g(x) = \sqrt{\ln(3x) + e^{\sin x}}$$

- 2 marks 2. (a) Evaluate the following two quantities

$$\sin\left(\frac{2\pi}{3}\right) \text{ and } \cos\left(\frac{2\pi}{3}\right)$$

- 5 marks (b) Find the equation of the tangent line to

$$f(x) = \frac{\cos x}{\sin x}$$

at the point $x = 2\pi/3$.

3. Show all relevant limit computations.

3 marks

(a) Find the equation(s) of all horizontal asymptotes of the following function

$$f(x) = \frac{5}{e^{-x} + 7}.$$

5 marks

(b) Find the equation(s) of all vertical asymptotes of the following function

$$g(x) = \frac{|x - 2|}{x^2 - 2x - 3}.$$

For each vertical asymptote determine whether each corresponding one sided limit equals $+\infty$ or $-\infty$.

1 mark

4. (a) Given function $f(x)$ state the definition of its derivative.

4 marks

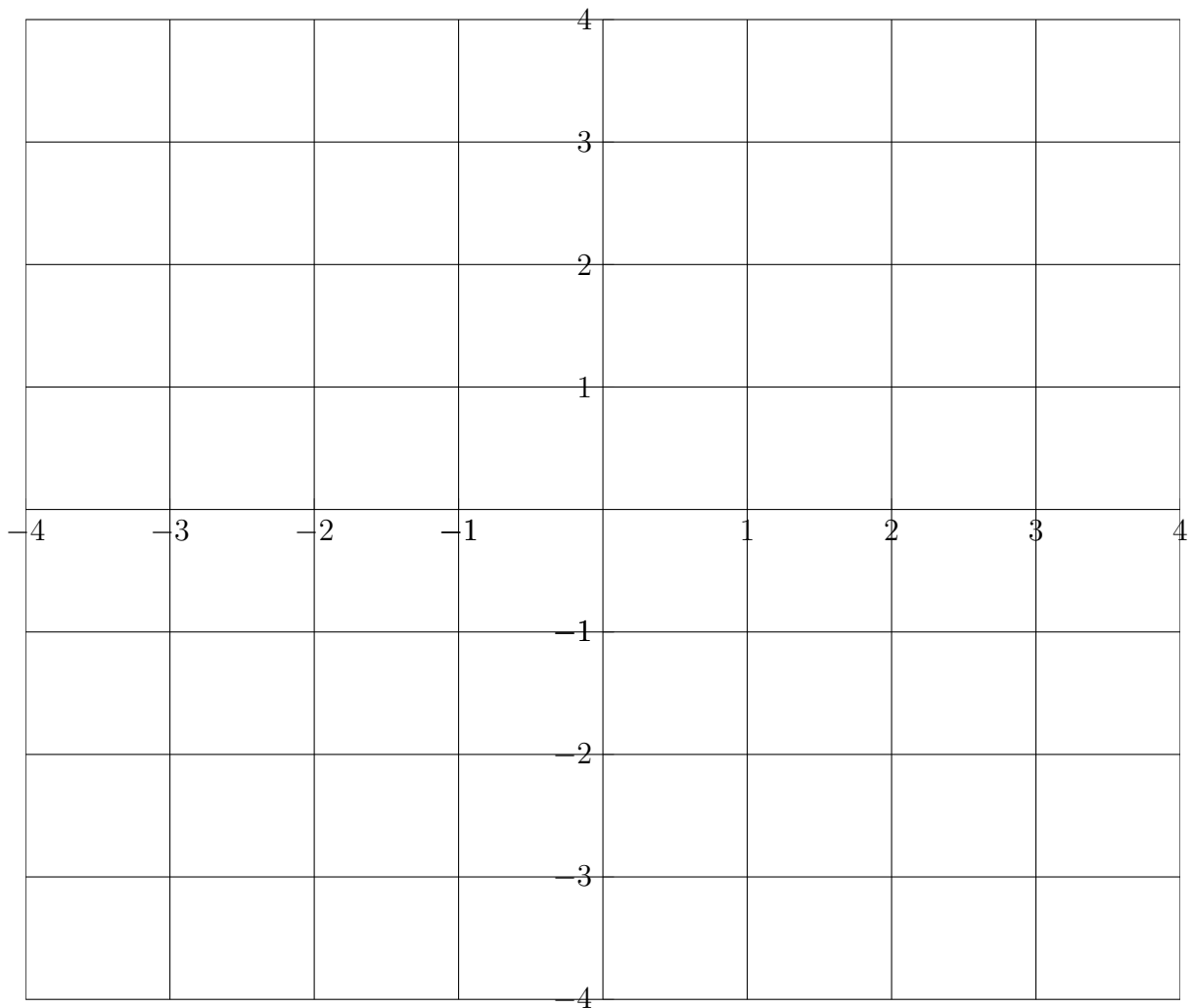
(b) Explain why your expression in part (a) should give you the slope of the tangent line to $f(x)$ at point x . Consider including a picture with your explanation.

6 marks

5. Sketch the graph of a function satisfying the following properties:

- The domain of $f(x)$ is $\{x \in \mathbb{R} : -4 \leq x \leq 4\}$
- $f(x)$ has a vertical asymptote at $x = -1$
- $\lim_{x \rightarrow -1^+} f(x) = 2$
- $\lim_{x \rightarrow 1} f(x)$ does not exist
- $f'(3) = 0$
- $f'(-3) = -1$

You do not need to find an equation for your function. Use the axes below.



There is another set of axes on the following page (in case you ruin the first one).

Extra axes:

