Students should be able to do the following by the end of each respective unit. Additions will be made as the term progresses.

Weeks 1, 2, 3: Review of Functions

We review the following in weeks 1, 2 and 3. Students will need to perform these tasks throughout the term as we study calculus.

- 1. Find the equation of a line (either in y = mx + b or $y y_1 = m(x x_1)$ form) given two points or one point and the slope.
- 2. Plot a line given its equation (including x and y intercepts).
- 3. Find the roots of a quadratic equation either by factoring or quadratic formula.
- 4. Plot the graphs of x^2 , x^3 , $\sin x$, $\cos x$, $\tan x$, e^x , b^x , $\ln x$, $\log_b x$. Plot the graph of a piecewise function with simple parts.
- 5. Explain what a function is.
- 6. Find the domain of rational functions and functions involving square roots.
- 7. Recognize a given function as a composition of two (or more) simpler functions.
- 8. Use the unit circle and/or special triangles to compute sine, cosine and tangent of special angles as well as solve equations involving sine, cosine and tangent.
- 9. Simplify expressions involving exponents or logarithms using exponent or logarithm rules.
- 10. Solve equations involving exponents or logarithms by recognizing b^x and $\log_b x$ as inverses.

Week 4: Limits

- 1. Explain using a picture what $\lim_{x\to a} f(x) = L$ means.
- 2. Explain using a picture what $\lim_{x\to a^-} f(x) = L$ and $\lim_{x\to a^+} f(x) = L$ means.
- 3. Evaluate limits using the graph of a function.
- 4. Evaluate limits of simple rational functions.
- 5. Given a rational function find the equations of any vertical and horizontal asymptotes.

Week 5: Definition of the Derivative

- 1. State the limit definition of the derivative.
- 2. Explain (using a picture) why the expression

$$\lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

should give the slope of the tangent line to f(x) at given point x.

3. Use the limit definition of the derivative to find the derivative of simple functions: polynomials, rational functions, functions with square roots.

Week 6: Derivative Rules

- 1. Use Power Rule to find the derivative of polynomials.
- 2. Compute the derivatives of sine, cosine and exponential functions.
- 3. Use Produce Rule and Quotient Rule to compute the derivatives of functions which are combinations of polynomials, trig functions, exponential functions.
- 4. Demonstrate the consistency between Power, Product and Quotient rules.
- 5. Use the derivative to find the slope and equation of tangent lines.
- 6. Find where a given function has horizontal tangent lines.

Week 7 and 8: Chain Rule and Related Rates

- 1. Compute the derivatives of compositions of functions using chain rule.
- 2. Combine chain rule with other differential rules (including chain rule itself) to compute the derivative of more complicated functions (involving: polynomials, exponential functions, logarithms, trig functions).
- 3. Find the equations of tangent lines of above mentioned functions.
- 4. Solve simple related rates problems using a systematic method of enumerated steps.

Week 9: Integrals and Riemann Sums

- 1. Approximate the area under a curve using a finite number of Riemann Sums. In simple cases argue why such an approximation may be an overestimate or an underestimate.
- 2. Explain using a picture why the expression

$$\lim_{n \to \infty} \sum_{i=1}^{n} f(x_i) \Delta x$$

should give exactly the area under the curve f(x). Indicate on your picture what $n, x_i, f(x_i)$ and Δx are.

- 3. Express the area of a given shape as an integral. For example express the area of a circle as an integral or express the area under the curve $f(x) = \sin 2x$ over a full period as an integral.
- 4. For a given simple function, explain, given the steps, the computation of

$$\lim_{n \to \infty} \sum_{i=1}^{n} f(x_i) \Delta x$$

by taking the limit as $n \to \infty$.

Week 10: Definite and Indefinite Integrals

1. State the following part of the Fundamental Theorem of Calculus

$$\int_{a}^{b} f(x)dx = F(b) - F(a)$$

explaining what F(x) is.

- 2. Use integral rules to simplify/evaluate integrals.
- 3. Compute definite integrals of polynomials, trig functions and the exponential function.
- 4. Find the indefinite integral (general anti-derivative) of polynomials, trig functions and the exponential function.
- 5. Given a function, find the specific anti-derivative satisfying a certain condition.
- 6. Explain why a function has more than one anti-derivative.

Week 11: Method of Substitution

- 1. Perform the method of substitution to compute definite and indefinite integrals.
- 2. Identify possibilities for a substitution and demonstrate their usefulness/un-usefulness.
- 3. Explain, using an example, why substitution is the opposite of chain rule.

Week 12: Integration by Parts and Applications of Integrals

- 1. Compute definite/indefinite integrals using Integration by Parts.
- 2. Explain, using an example, why integration by parts is the opposite of product rule.
- 3. Solve simple physics problems, involving displacement, velocity and acceleration, using antiderivatives.