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Dec-4

Grab a Survey  $\longrightarrow$

Final Exams: Dec. 14 (Monday)  
at 12 noon in LSk 201  
2.5 hours.

Regular office hours Today: (1-3pm)

Exam office hours: (in LSk 300C)

Thurs. (10 <sup>th</sup> )	2-4pm
Fri. (11 <sup>th</sup> )	12-3pm (Jan 2-3)
Sat. (12 <sup>th</sup> )	1-3pm (Jan 2-3)

- Course Evaluations ; do them.
- Solutions to HW11 posted.
- All assignments / quizzes returned.
- All grades posted - no names?  
- term grade posted today.
- Exam practice posted today.

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- Review:
- unit circle, trig.
  - $e^x$ ,  $\ln x$
  - $x^2 x^3 = x^5$ .

Topics:

- Limits
  - asymptotes
  - Definition of Derivative
- } not on exam.

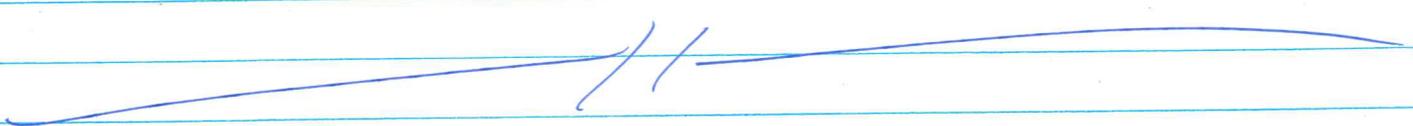
• ~~Def~~ Derivative Rules.

power/product/quotient/chain      tangent line computations.

Eg.  $(x e^{\sin x})'$

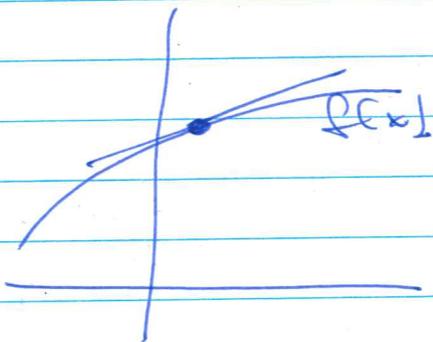
$$= (x)' e^{\sin x} + x (e^{\sin x})'$$
$$= e^{\sin x} + x e^{\sin x} \cos x$$

- Related Rates.
- Riemann Sums.
- Definite/Indefinite Integrals.
- Substitution
- Integration by Parts.
- "Word Problem"
- Expect a "Synthesis" question where you are asked to draw a function.



Where does math go /  
what do I do all day?

### Differential Calc.



Find tangent line.  
• Needed derivatives

$$\frac{df}{dx}$$

### Integral Calc.

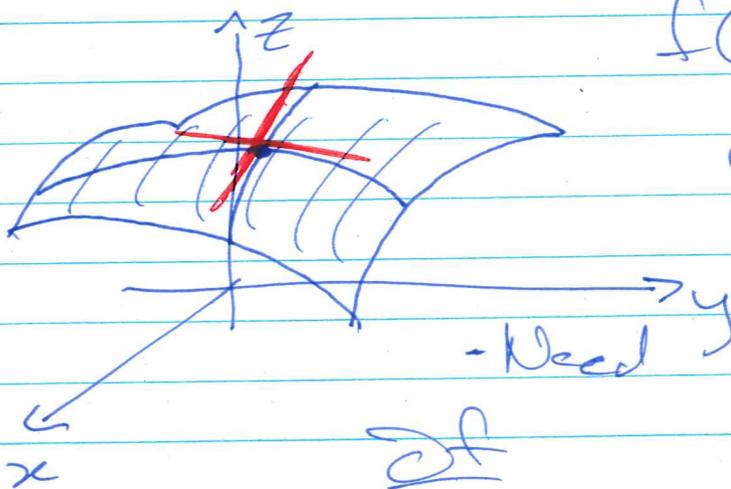


Find area.

• Needed integral

$$\int f(x) dx$$

### Multi-variable Calculus:



$$f(x, y)$$

Can have tangent lines in multiple directions

- Need Partial derivatives.

$$\frac{\partial f}{\partial x}$$

$$\frac{\partial f}{\partial y}$$

## Differential Equations:

Eg. : •  $f'(x) = f(x)$   
Find  $f(x)$  satisfying the equation  
 $f(x) = e^x$

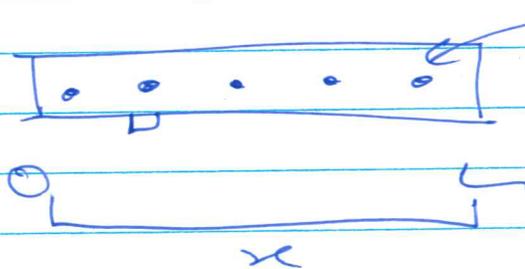
•  $f''(x) = -f(x)$   
 $f(x) = \pm \cos x$  or  $\pm \sin x$

•  $f''(x) - 5f'(x) + 6f(x) = 0$   
 $f(x) = e^{3x}$  or  $e^{2x}$

## Partial Differential Equations: (this is what I do).

Eg. heat in a rod temperature depends on  $x$  and time.

heat  
↓



$u(x, t)$

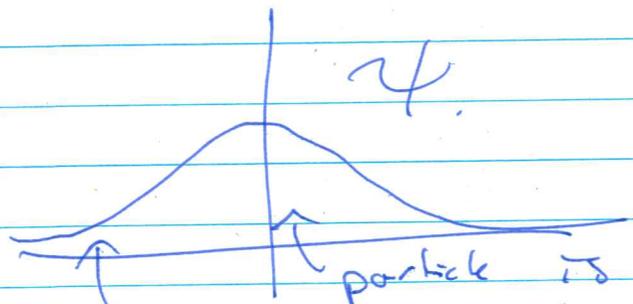
Heat Eq.  $\frac{\partial u}{\partial t} = c^2 \frac{\partial^2 u}{\partial x^2}$

# I study the Nonlinear Schrödinger Equation.

Linear! 
$$i \frac{\partial \psi}{\partial t} = -\frac{\partial^2 \psi}{\partial x^2} + V \psi$$

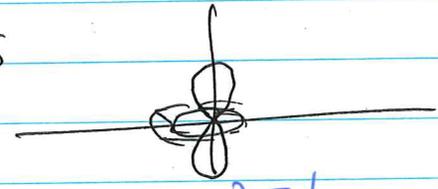
↑ external force

$$\psi = \sqrt{|\psi|^2}$$



particle is probably in the middle  
might be here but probably not.

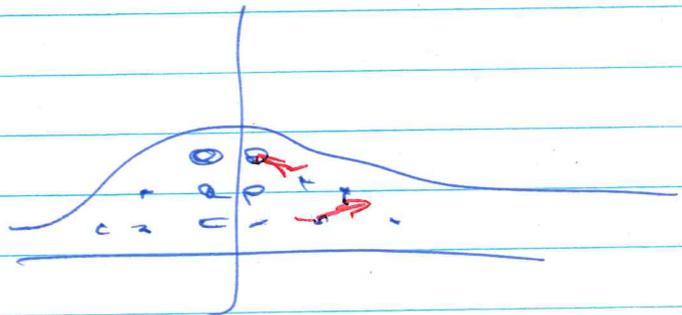
- analysis of this gives the orbital shapes



Nonlinear! 
$$i \frac{\partial \psi}{\partial t} = -\frac{\partial^2 \psi}{\partial x^2} \pm |\psi|^2 \psi$$

Many particles

+ is particles don't like each other  
- particles do.



What is happening.