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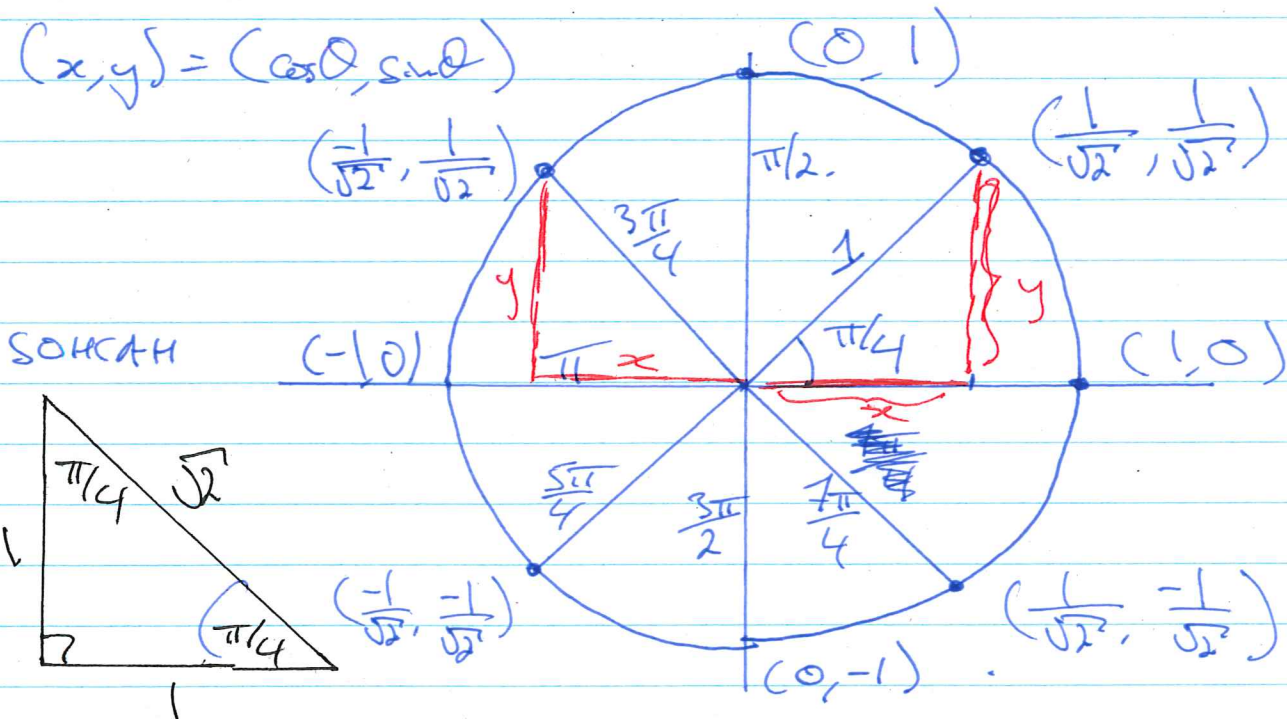
• HW1 Due Monday.

• Thursday Lab CIB moved to  
MATX 1100. Each week.  
Math Annex.

- MLC into Friday.
- Quiz #1 ~~Friday~~ into Friday.  
Quiz #1 Friday 25<sup>th</sup>.

Let's go around the unit circle in multiples of  $\pi/4$ :

$$(x, y) = (\cos \theta, \sin \theta)$$



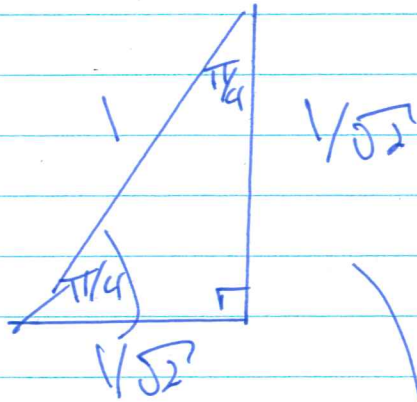
0,  $\pi/4$ ,  $2\pi/4$ ,  $3\pi/4$ ,  $4\pi/4$ ,  $5\pi/4$ ,  $6\pi/4$ ,  $7\pi/4$   
 "  $\pi/2$  "  $\pi$  "  $3\pi/2$

(aside:  $\frac{\sqrt{2}}{\sqrt{2}} \cdot \frac{\sqrt{2}}{2}$  vs.  $\frac{1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}}$ )

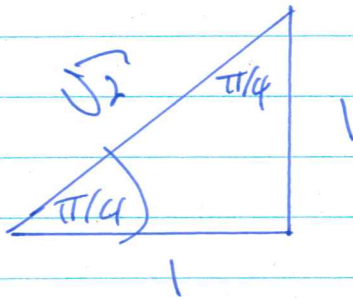
2

1 side!

$$\cos\left(\frac{\pi}{4}\right) = \frac{1}{\sqrt{2}}$$



Similar triangles.



$$\cos\left(\frac{\pi}{4}\right) = \frac{1}{\sqrt{2}}$$

3

Now let us go around in multiples of  $\pi/6$ :

Students

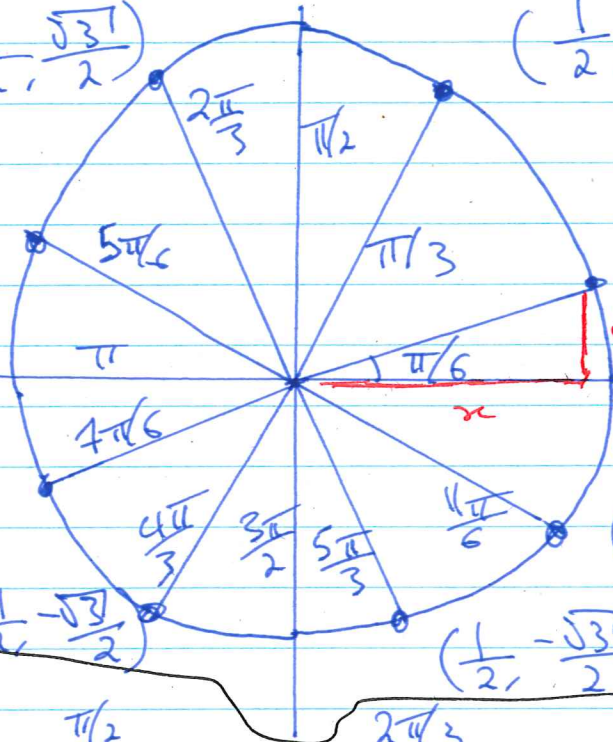
$(-\frac{1}{2}, \frac{\sqrt{3}}{2})$

$(\frac{1}{2}, \frac{\sqrt{3}}{2})$

All

$(-\frac{\sqrt{3}}{2}, \frac{1}{2})$

$(\frac{\sqrt{3}}{2}, \frac{1}{2})$



$(-\frac{\sqrt{3}}{2}, -\frac{1}{2})$

$(\frac{\sqrt{3}}{2}, -\frac{1}{2})$

Take

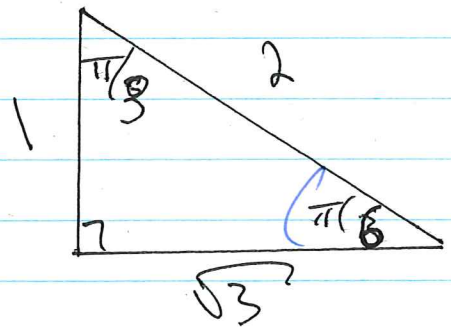
$(-\frac{1}{2}, -\frac{\sqrt{3}}{2})$

$(\frac{1}{2}, -\frac{\sqrt{3}}{2})$

Calculus

- $\pi/6$
- $\frac{2\pi}{6}$
- $\frac{3\pi}{6}$
- $\frac{4\pi}{6} = 2\pi/3$
- $\frac{5\pi}{6}$
- $\frac{6\pi}{6} = \pi$

- $\frac{7\pi}{6}$
- $\frac{8\pi}{6}$
- $\frac{9\pi}{6}$
- $\frac{10\pi}{6}$
- $\frac{11\pi}{6}$
- "
- $\frac{4\pi}{3}$
- $\frac{3\pi}{2}$
- $\frac{5\pi}{3}$

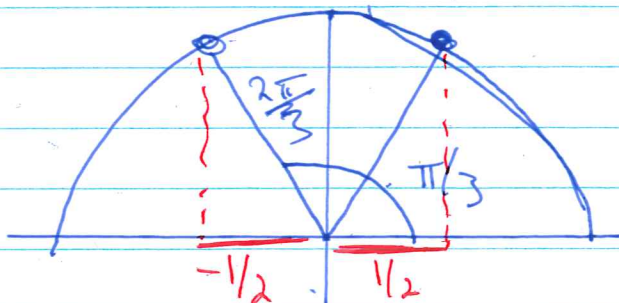




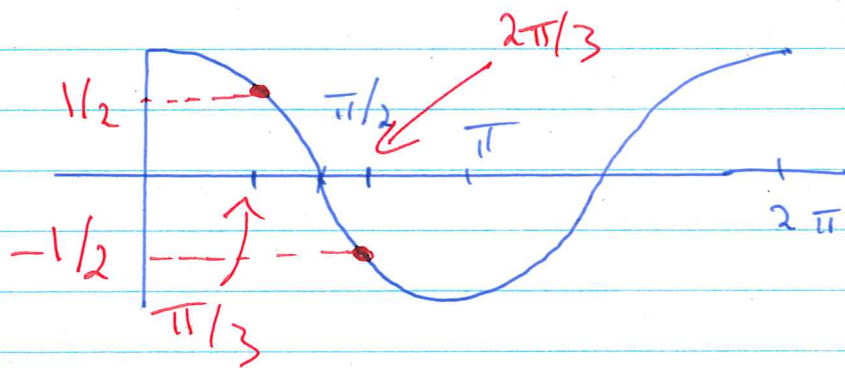
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Last class we wanted to find

$$\cos\left(\frac{2\pi}{3}\right)$$



$$\cos\left(\frac{2\pi}{3}\right) = -\cos\left(\frac{\pi}{3}\right) = -1/2$$



Example: Find  $x$  in  $[0, 2\pi)$  satisfying:

$$2 \sin x \cos x + \cos x = 0$$

$$(\cos x)(2 \sin x + 1) = 0$$

$$\Rightarrow \cos x = 0 \quad \text{or} \quad 2 \sin x + 1 = 0$$

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aside:

$$yx + x = 0$$

$$x(y+1) = 0$$

$$x=0, \quad y=-1$$

When does  $\cos x = 0$  ?

$$x = \pi/2, \quad 3\pi/2$$

When does  $2 \sin x + 1 = 0$

$$2 \sin x = -1$$

$$\sin x = -1/2$$

$$\text{So, } x = \frac{7\pi}{6}, \quad \frac{11\pi}{6}$$

$$\Rightarrow x = \pi/2, \quad 3\pi/2, \quad 7\pi/6, \quad 11\pi/6$$

Example: Find values in  $[0, 2\pi)$   
where

$$2 \cos x \sin x + \sqrt{3} \cos x = 0$$

$$\cos x (2 \sin x + \sqrt{3}) = 0$$

$$\Rightarrow \cos x = 0$$

$$2 \sin x + \sqrt{3} = 0$$

$$\sin x = \frac{-\sqrt{3}}{2}$$

$$\Rightarrow x = \pi/2, \quad 3\pi/2$$

$$x = \frac{4\pi}{3}, \quad \frac{5\pi}{3}$$