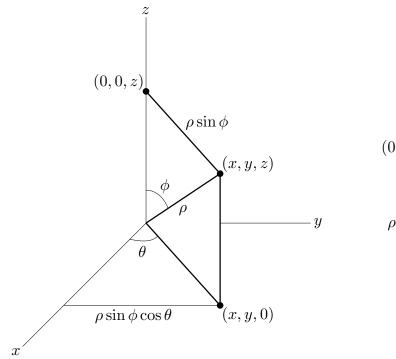
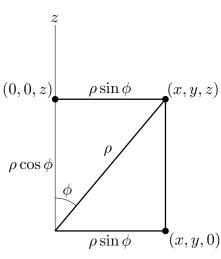
## SPHERICAL COORDINATES





Side View

 $\rho = \text{ distance from } (x, y, z) \text{ to } (0, 0, 0)$ 

 $\phi = \text{ angle between the line } \overline{(0,0,0)\,(x,y,z)} \text{ and the } z \text{ axis}$ 

 $\theta = \text{ angle between the line } \overline{(0,0,0)\,(x,y,0)} \text{ and the } x \text{ axis}$ 

$$x = \rho \sin \phi \cos \theta$$

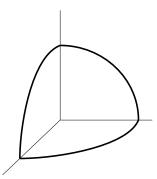
$$p = \sqrt{x^2 + y^2 + z^2}$$

$$y = \rho \sin \phi \sin \theta$$

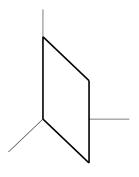
$$\theta = \tan^{-1} \frac{y}{x}$$

$$z = \rho \cos \phi$$

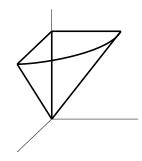
$$\phi = \tan^{-1} \frac{\sqrt{x^2 + y^2}}{z}$$



surface of constant  $\rho$ 



surface of constant  $\theta$ 



surface of constant  $\phi$