

Wednesday, February 25

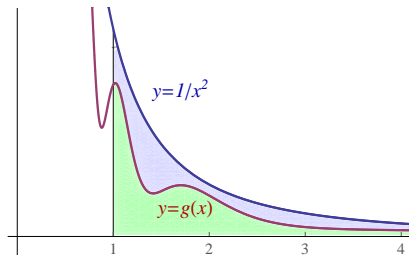
Clicker Questions

Clicker Question 1

Comparing two improper integrals

We saw on Monday that $\int_1^{\infty} \frac{1}{x^2} dx$ is convergent. Suppose that $0 \leq g(x) \leq \frac{1}{x^2}$ for all $x \geq 1$. What do you think we can say about

$$\int_1^{\infty} g(x) dx?$$

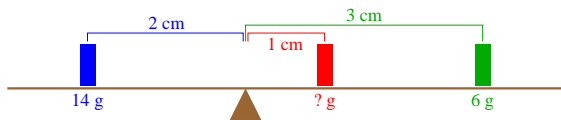


- A. impossible to tell, even with the formula for $g(x)$
- B. might be convergent or divergent, depending on the formula for $g(x)$
- C. has a negative value
- D. **definitely convergent**
- E. definitely divergent

Clicker Question 2

Just a moment

A 6-gram object is placed 3 cm to the right of the origin, and a 14-gram object is placed 2 cm to the left of the origin. How much mass must be placed 1 cm to the right of the origin to make the **total moment** (with respect to the origin) **equal to 0**?



- A. 5 grams
- B. 10 grams
- C. 44 grams
- D. 8 grams
- E. none of the above

Clicker Question 3

A massive undertaking

A lamina with density $\rho = 4$ is in the shape of the region between the graphs of $y = 1/x$ and $y = (3 - x)/2$. Find the **mass of the lamina**.

- A. $3 - 4 \ln 2$
- B. $\ln 2 - 3/4$
- C. $3/4 - \ln 2$
- D. $4 \ln 2 - 3$
- E. none of the above

The calculation

Setting the two functions equal, we find that the graphs intersect at $x = 1$ and $x = 2$.

So the mass is

$$4 \int_1^2 \left(\frac{3-x}{2} - \frac{1}{x} \right) dx.$$