

**Math 323, Homework 8, Due Tuesday March 18.**

**1.** Let  $F$  be a field, and  $V_1, V_2$  be finite-dimensional  $F$ -vector spaces. Prove that the  $F[x]$ -module  $(V_1, T_1)$  is isomorphic to the  $F[x]$ -module  $(V_2, T_2)$  if and only if  $\dim V_1 = \dim V_2$  and there exists a basis  $\{\bar{e}_1, \dots, \bar{e}_n\}$  of  $V_1$  and a basis  $\{\bar{w}_1, \dots, \bar{w}_n\}$  of  $V_2$  such that the matrix of  $T_1$  with respect to the basis  $\{\bar{e}_i\}$  coincides with the matrix of  $T_2$  with respect to the basis  $\{\bar{w}_i\}$ .

**Section 10.1:** Problems 7, 8, 9, 10, 11, 20.

**Section 10.2:** Problems 4, 6, 8.