

**Final exam for Math 534.**

1. Prove the global existence and uniqueness theorems for connected semisimple algebraic groups. (You can use any facts that we have *proved* in class).
2. Prove that the simply connected cover of  $\mathrm{SO}_3(\mathbb{C})$  is the group  $\mathrm{SL}_2(\mathbb{C})$ .
- 3.\* Prove that the simply connected cover of  $\mathrm{SO}_5(\mathbb{C})$  is  $\mathrm{Sp}_4(\mathbb{C})$ .