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Cor. X, Y . $X \perp Y$, $|X| = 1 = |Y|$

$$K(X, Y) - \bar{K}(X, Y) = g(\alpha(X, X), \alpha(Y, Y)) - |\alpha(X, Y)|^2$$

Cor. If \bar{M} has constant sectional curvature K , then

$$R(X, Y)Z = K(g(Y, Z)X - g(X, Z)Y) - \frac{\alpha}{2}(X, Y)Z$$

If $\bar{M} = \mathbb{R}^{n+k}$ with flat metric, then

$$R(X, Y) = -\frac{\alpha}{2}(X, Y)$$

Ex. $M^n \subset \mathbb{R}^{n+1}$. $Ax_i = \lambda_i x_i$. x_i o.n.

$\xi \uparrow$
 $|x_i| = 1$

$$R(x_i, x_j)x_k = g(Ax_j, x_k)Ax_i - g(Ax_i, x_k)Ax_j$$

$$= \lambda_i \lambda_j \delta_{jk} x_i - \lambda_i \lambda_j \delta_{ik} x_j$$

$$= \begin{cases} 0 & k \neq i, j \\ -\lambda_i \lambda_j x_j & k = i \\ \lambda_i \lambda_j x_i & k = j \end{cases}$$

$$\therefore R(x_i, x_j) \rightarrow \begin{matrix} & i & j \\ i & & \lambda_i \lambda_j \\ j & -\lambda_i \lambda_j & \end{matrix}$$