Math 427/527: algebraic topology
Homework problem for Lecture 17.

Read Hatcher's Section 3.2.

By explicitly calculating the ring structure on cohomology in each case, prove that $S^5 \times S^2$ and $S^7 \vee S^5 \vee S^2$ are not homotopy equivalent.