# MATH 100 - WORKSHEET 20 <br> RELATED RATES 

1. Related rates
(1) Two ships are travelling near an island. The first is located 20 km due west of it and is moving due north at $5 \mathrm{~km} / \mathrm{h}$. The second is located 15 km due south of it and is moving due south at $7 \mathrm{~km} / \mathrm{h}$. How fast is the distance between the ships changing?
(2) The same setting, but now the first ship is moving toward the island.
(3) A conical drain is 6 m tall and has radius 1 m at the top.
(a) The drain is clogged, and is filling up with rain water at the rate of $5 \mathrm{~m}^{3} / \mathrm{min}$. How fast is the water rising when its height is 5 m ?
(b) Once the drain is unclogged the water begins to clear at the rate of $15 \mathrm{~m}^{3} / \mathrm{min}$ (but rain is still falling!). At what height is the water falling at the rate of $40 \mathrm{~m} / \mathrm{min}$.
