

Math 322: Introduction to Group Theory

Lecture 1

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Groups ???

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Abstract
algebra

1 About the
course

2 Learning
methods

3 About me

- Algebraic Structure = Underlying set + operations + axioms

Math 223,412	Math 322	Math 323	Math 422
Vector space	Group	Ring	Field
Subspace	Subgroup	Subring, ideal	Subfield
Linear map	Homomorphism		Field embedding
Spanning set	Set of generators		

Galileo says

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Philosophy is written in that great book (I mean the universe) ... but the book cannot be understood unless one first learns the language and the symbols in which it is written. This book is written in the mathematical language ... without whose help it is impossible to comprehend a single word of it; without which one wanders in vain through a dark labyrinth.

— Galileo Galilei, *The Assayer*, 1623.

- Vector space: state space of QM system, space of signals. space of codewords, tangent space to manifold, ...
- Group = symmetries of a shape, a number system, ...

Today's Goals

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- 1 About of the course
- 2 Learning methods
- 3 About me
- 4 A concrete group

Learning goals

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- D Computations in concrete groups
Basic notions, axioms, and basic implications.
- C Definitions, Theorems, basic calculations in
abstract groups
- B Can work in abstract groups
- A Mastery of course material
- A+ Problem-solving

Course plan

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1 About the
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- Concrete Groups
- Groups and Homomorphisms
- Group Actions
- Sylow's Theorems
- Solvable and Nilpotent groups

Components of the course

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- Classes (TTh 14:00-15:30, LSK 460)
- Written homework (generally due Thursdays) [25%]
 - First problem set due September 14
- Weekly online homework (due 9pm on Tuesdays) [5%]
 - First WebWork due September 19
- Midterm exam October 17 [20%]
- Final exam [50%]

MUST SCORE 80% ON CONCRETE COMPUTATIONS TO PASS (Unlimited retakes for midterm)

- Office Hours

About me

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3 About me

- Dr. Lior Silberman (Li'or Zilberman)
- Email: lior@math.ubc.ca, Office: MATH 229B.
- Work: Number Theory, PDE, Topology, Random Structures, ...

